

***** Mathematical Weekly *****
(week nine)

1	$= 1^2$
1 + 3	$= 2^2$
1 + 3 + 5	$= 3^2$
1 + 3 + 5 + 7	$= 4^2$
1 + 3 + 5 + 7 + 9	$= 5^2$
1 + 3 + 5 + 7 + 9 + 11	$= 6^2$
1 + 3 + 5 + 7 + 9 + 11 + 13	$= 7^2$

1	= 1^3
3 + 5	= 2^3
7 + 9 + 11	= 3^3
13 + 15 + 17 + 19	= 4^3
21 + 23 + 25 + 27 + 29	= 5^3
31 + 33 + 35 + 37 + 39 + 41	= 6^3
43 + 45 + 47 + 49 + 51 + 53 + 55	= 7^3

$$\begin{array}{rcl}
 2^0 & + & 2^0 = 2^1 \\
 2^1 & + & 2^1 = 2^2 \\
 2^2 & + & 2^2 = 2^3 \\
 2^3 & + & 2^3 = 2^4 \\
 2^4 & + & 2^4 = 2^5 \\
 \\ \dots & & \dots \\
 3^0 & + & 3^0 + 3^0 = 3^1 \\
 3^1 & + & 3^1 + 3^1 = 3^2 \\
 3^2 & + & 3^2 + 3^2 = 3^3 \\
 3^3 & + & 3^3 + 3^3 = 3^4 \\
 3^4 & + & 3^4 + 3^4 = 3^5 \\
 \\ \dots & & \dots \\
 n^0 & + & n^0 + \dots + n^0 = n^1
 \end{array}$$

$$n^1 + n^1 + \dots + n^1 = n^2$$