

Overview of Signals and Systems

Chapter Intended Learning Outcomes:

- (i) Understand basic concepts of signals and systems
- (ii) Realize that signals and systems arise in our daily life

What is Signal?

- Anything that conveys **information**, e.g.,
 - Speech
 - Electrocardiogram (ECG)
 - Radar pulse
 - Traffic light
 - Medical image
 - Stock price
 - Orthogonal frequency division multiplexing waveform
 - Video
 - Smell

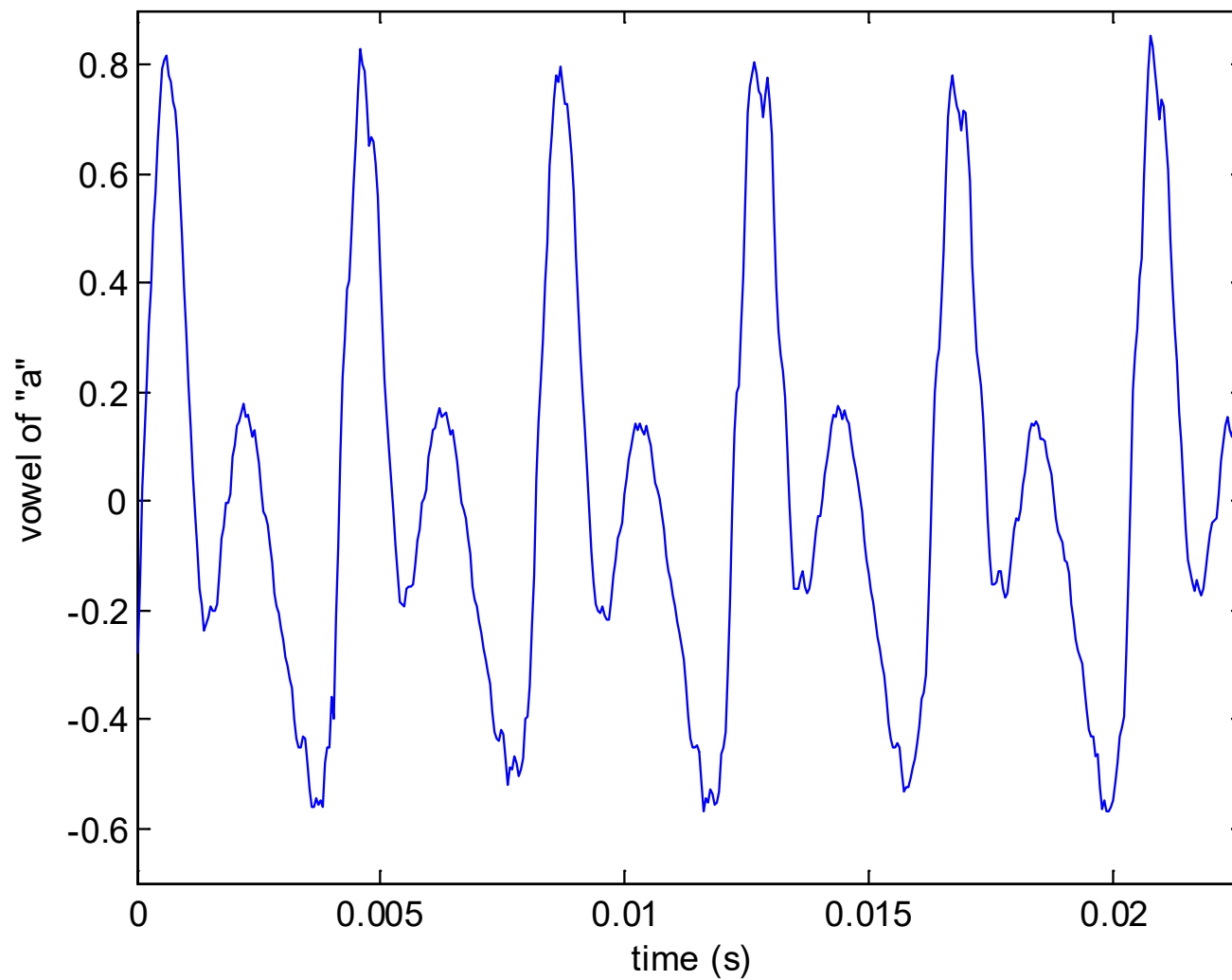


Fig.1.1: Speech

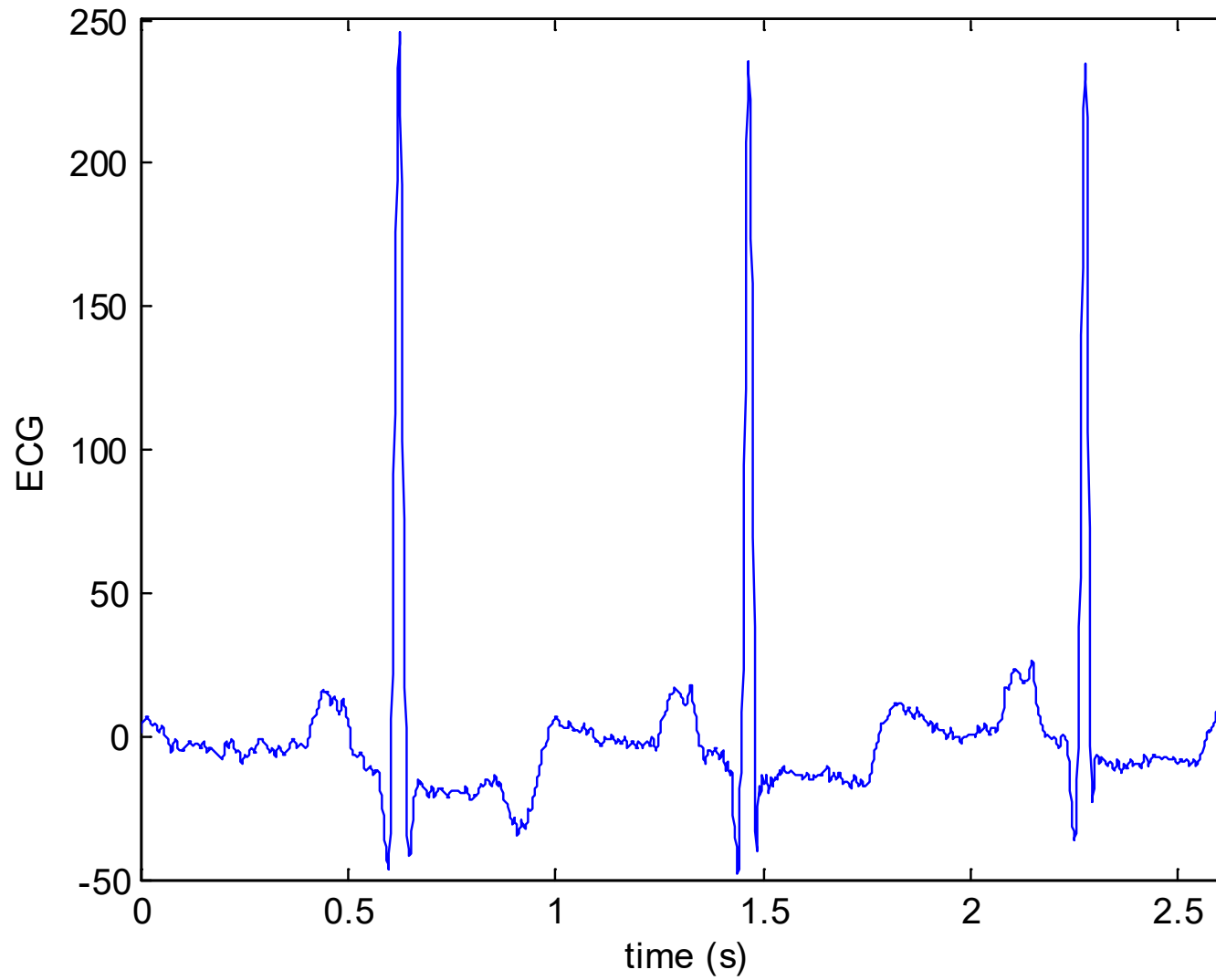
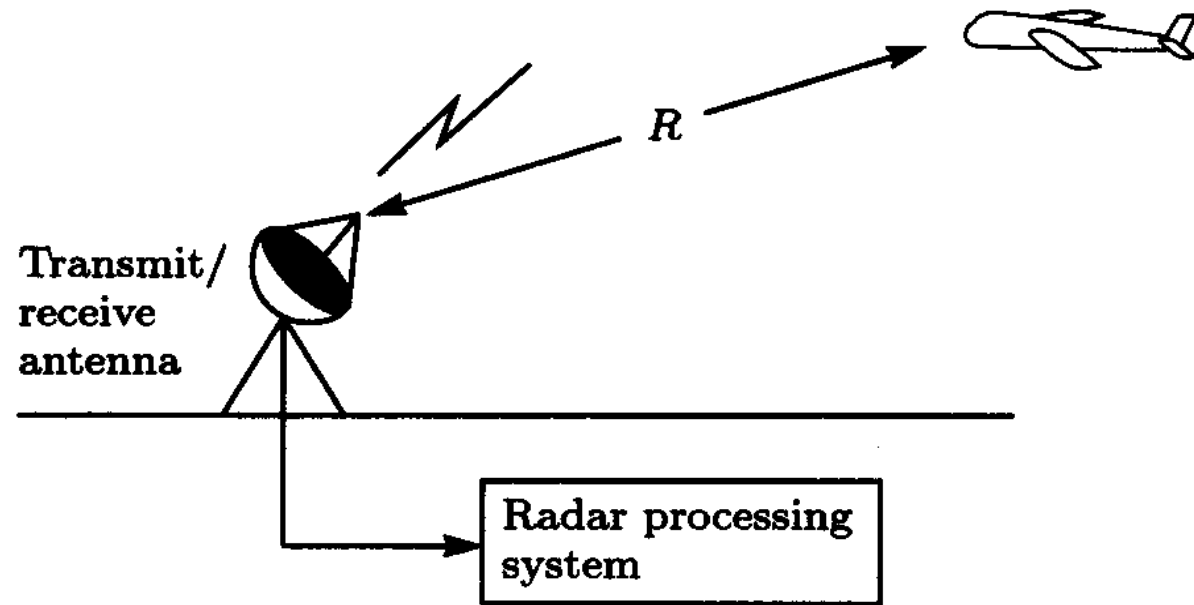


Fig.1.2: ECG



$$r(t) = s(t - \tau) + w(t)$$

Fig.1.3: Radar ranging

Given the signal propagation speed, denoted by c , the **time delay** τ is related to R as:

$$\tau = \frac{2R}{c} \quad (1.1)$$

Hence radar pulse contains the object **range** information.

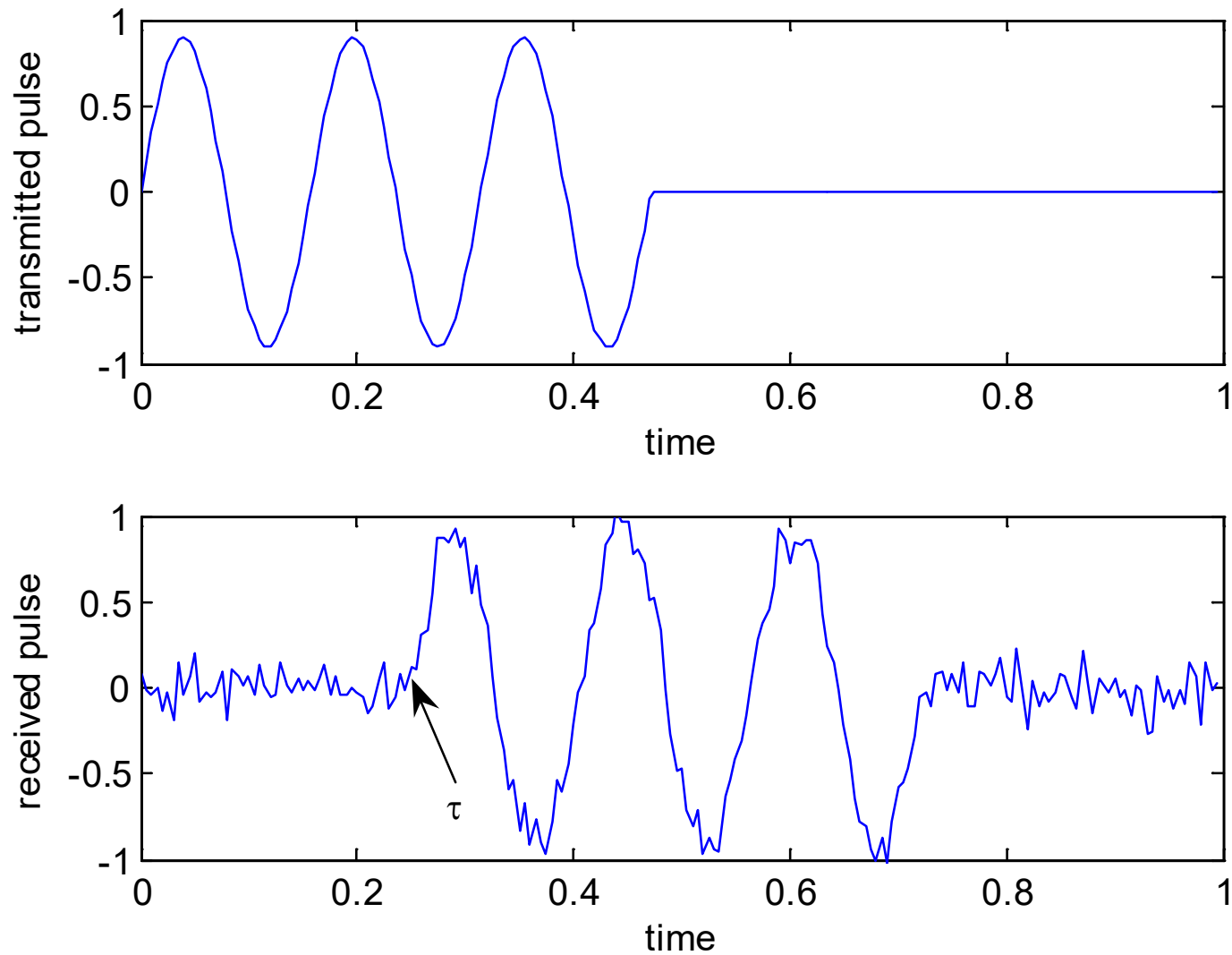


Fig.1.4: Transmitted & received radar waveforms: $s(t)$ & $r(t)$

- Can be a function of one, two or three independent variables, e.g., speech is one-dimensional (1-D) signal, function of time; image is 2-D, function of space; wind is 3-D, function of latitude, longitude and elevation.
- 3 types of signals that are functions of **time**:
 - **Continuous-time (analog)** $x(t)$: defined on a continuous range of time t , amplitude can be any value.
 - **Discrete-time** $x(nT)$ (**sampled**): defined only at discrete instants of time $t = \dots - T, 0, T, 2T, \dots$, amplitude can be any value.
 - **Digital (quantized)** $x_Q(nT)$: both time and amplitude are discrete, i.e., it is defined only at $t = \dots - T, 0, T, 2T, \dots$ and amplitude is confined to a finite set of numbers.

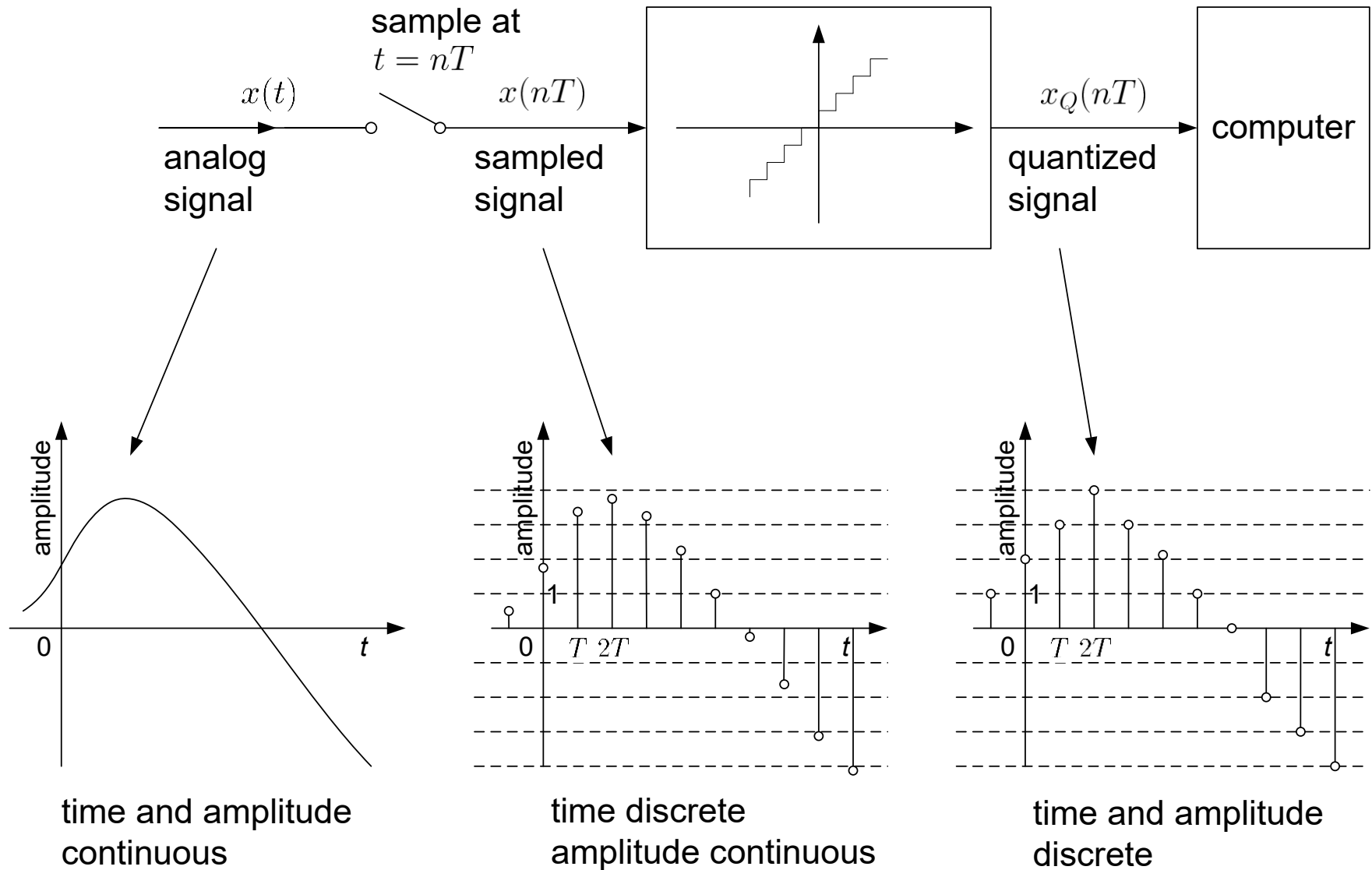


Fig. 1.5: Relationships between $x(t)$, $x(nT)$ and $x_Q(nT)$

$x(nT)$ at $n = 0$ is close to 2 and $x_Q(0) = 2$.

$x(nT) \in (3, 4)$ at $n = 1$ and $x_Q(T) = 3$.

Using 4-bit representation, $x_Q(0) = 0010$ and $x_Q(T) = 0011$, and in general, the value of $x_Q(nT)$ is restricted to be an integer between -8 and 7 according to the two's complement representation.

We focus on **continuous-time** and **discrete-time** signals. Discrete-time signal is also commonly represented by $x[n]$ with $n = \dots - 1, 0, 1, \dots$ being the time index.

In this course, we assume that $x(nT) = x_Q(nT)$, i.e., the quantizer has infinite or very high resolution.

What is System?

- Mathematical model or abstraction of a physical process that relates **input** to **output**:

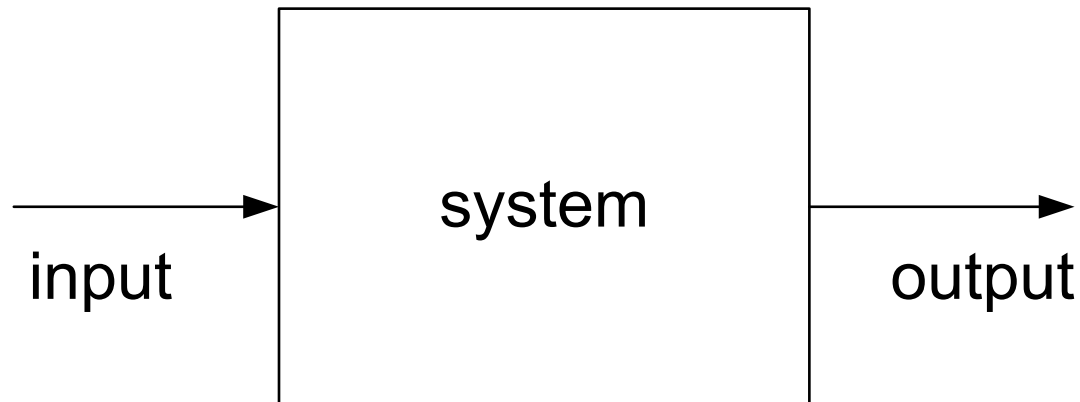


Fig.1.6: System with input and output

- It operates on an input to produce an output, e.g.:
 - Grading system: inputs are coursework and examination marks, output is grade.

- Squaring system: input is 5, then the output is 25.
- Amplifier: input is $\cos(\omega t)$, then output is $10 \cos(\omega t)$.
- Communication system: input to mobile phone is voice, output from mobile phone is 5G waveform.
- Noise reduction system: input is a noisy speech, output is a noise-reduced speech.
- Feature extraction system: input is $\cos(\omega t)$, output is ω .
- An **analog** or **continuous-time** system has continuous-time input and output while a **discrete-time** system deals with discrete-time input and output.
- A system can be realized in **hardware** or **software** via an algorithm.

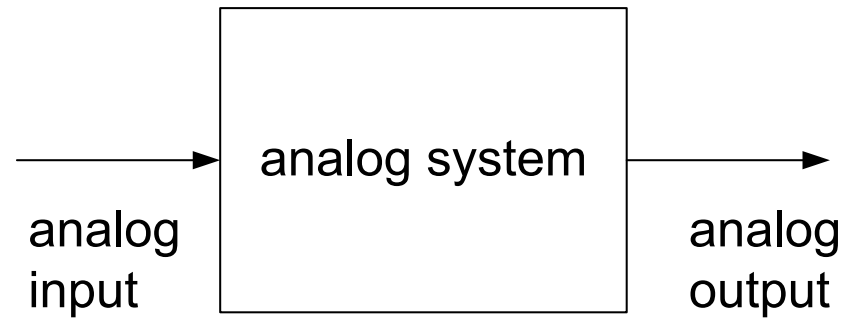


Fig.1.7: Continuous-time system

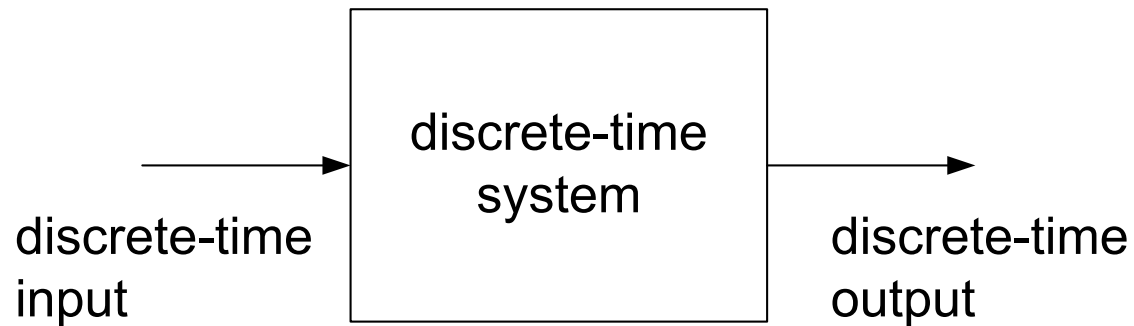


Fig.1.8: Discrete-time system

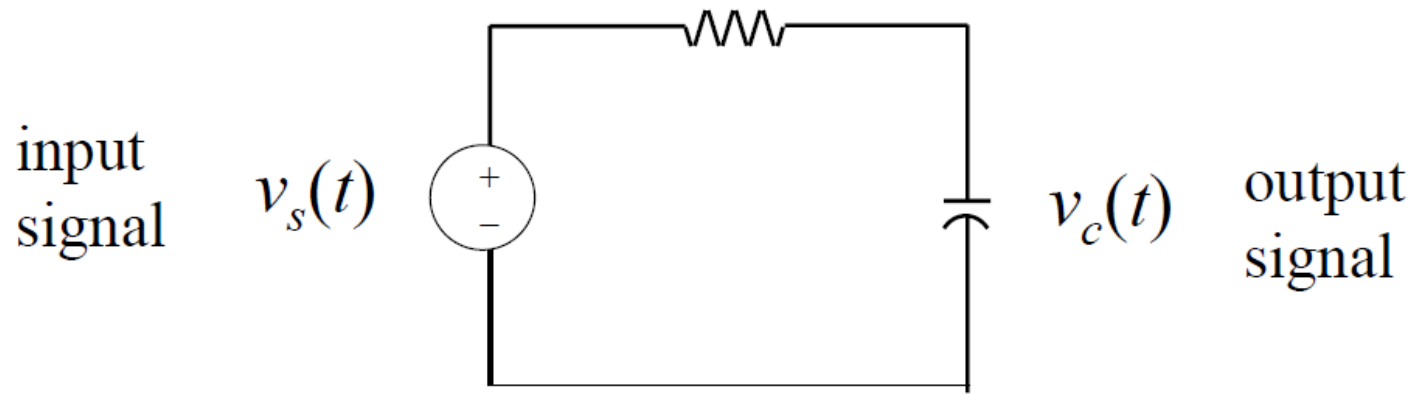


Fig.1.9: Hardware system of resistor-capacitor circuit

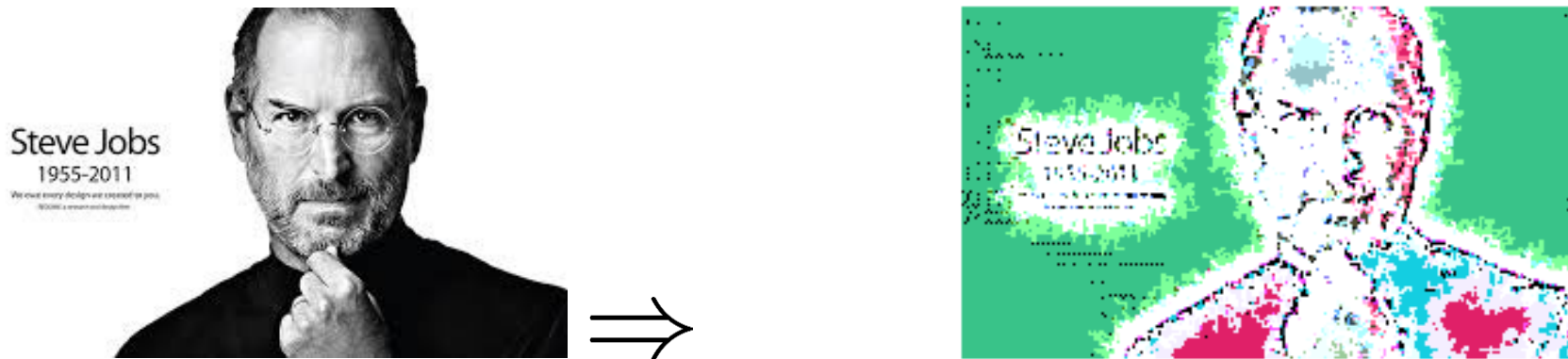


Fig.1.10: Pop-art production using an algorithm

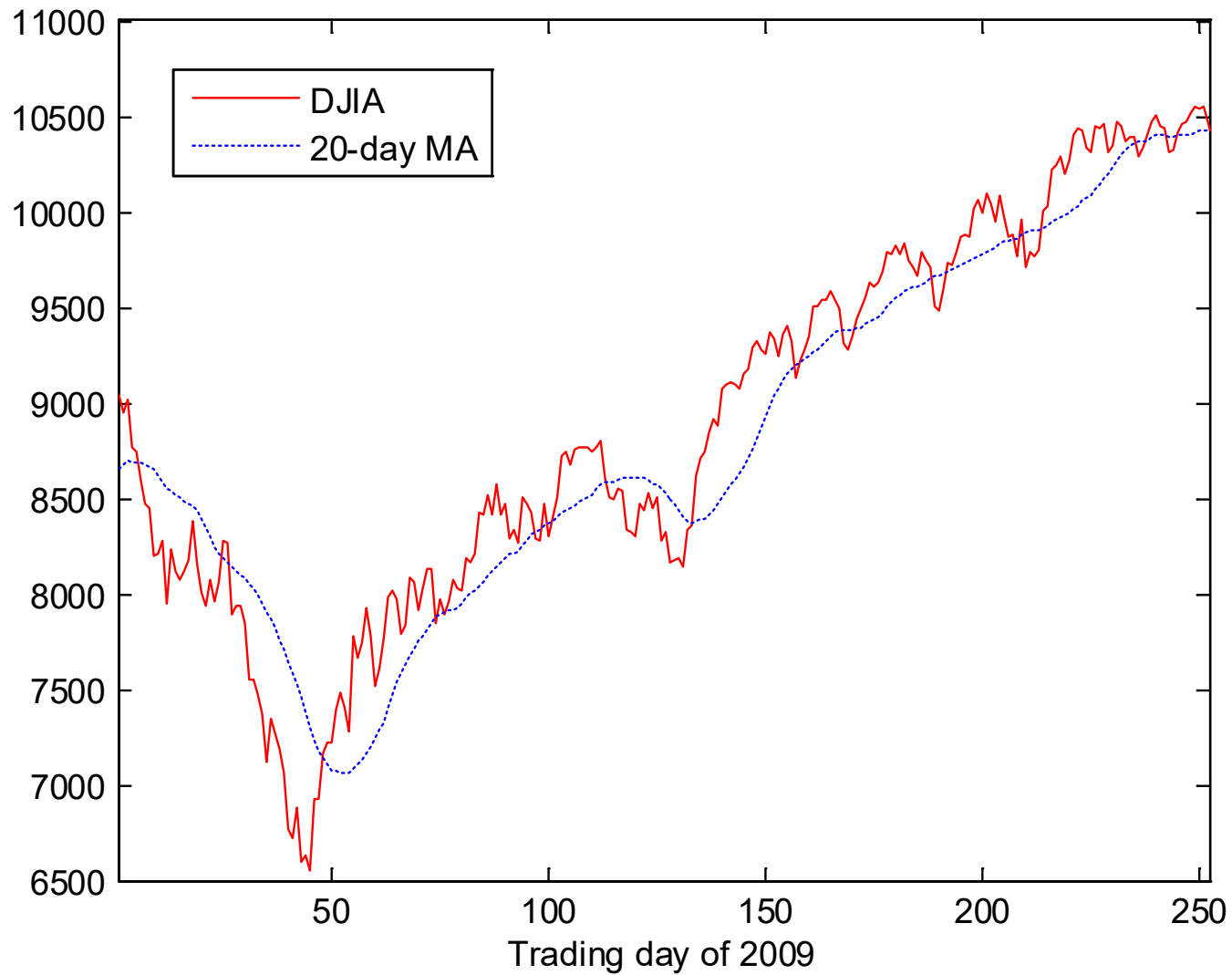


Fig.1.11: Software system for moving average of Dow Jones

Example 1.1

Consider an input signal $x(t) = \cos(\Omega t)$, for $t \in (-\infty, \infty)$, passing through a system. For $t < 0$, the system amplifies the input by 5, while for $t \geq 0$, the system squares the input, to produce the output $y(t)$.

Write down the mathematical expression of the system that relates $x(t)$ and $y(t)$. Is the input $x(t)$ continuous-time or discrete-time signal? Is the system continuous-time or discrete-time?

According to the system description, we obtain:

$$y(t) = \begin{cases} 5x(t), & t < 0 \\ x^2(t), & t \geq 0 \end{cases}$$

Moreover, the input is a continuous-time signal and the system is continuous-time.

What will You Learn?

- **Signal representation and characterization**, which includes generating signals, understanding signal types and properties, and performing operations on signals.
- **System classification and analysis**, which includes classifying system types, and calculating impulse response, frequency response, input and/or output for linear time-invariant (LTI) systems.
- **Transform tools** include Fourier series and Fourier transform as well as their applications in signal and LTI system analysis, e.g.: a periodic continuous-time signal $x(t)$ can be represented as sum of complex exponentials:

$$x(t) = \sum_{k=-\infty}^{\infty} a_k e^{jk\Omega_0 t}, \quad t \in (-\infty, \infty) \quad (1.2)$$

For a sinusoid $x(t) = 10 \cos(10t)$ which is a **time domain** signal, we can also view it in the **frequency domain**. Both represent the same signal.

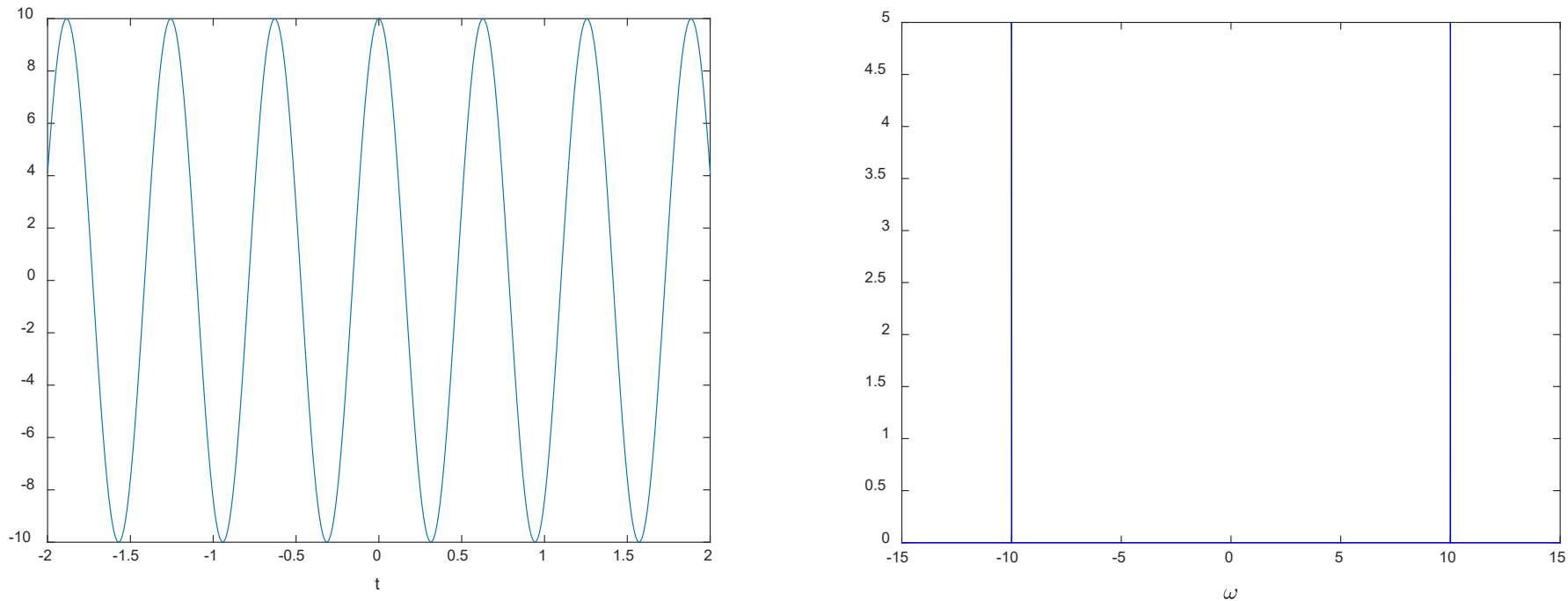


Fig.1.12: Sinusoid in time and frequency domains

Why Important?

- Signals and systems arise in our daily life, studying it will lay a good foundation for you in other relevant/higher-level courses and to solve real-world problems:
 - Generate signals which meet certain specifications, e.g., radar waveform, synthesized speech and music.
 - Analyze real-world process using a system point-of-view, e.g., moving average can be described as a system, characterized by input and output relationship.
 - Design and implement systems which produce desired outputs, e.g., a system which can compute the target range from radar waveforms
 - Analyze signals in the frequency domain, e.g., the speech segment in Fig.1.1 can be represented as:

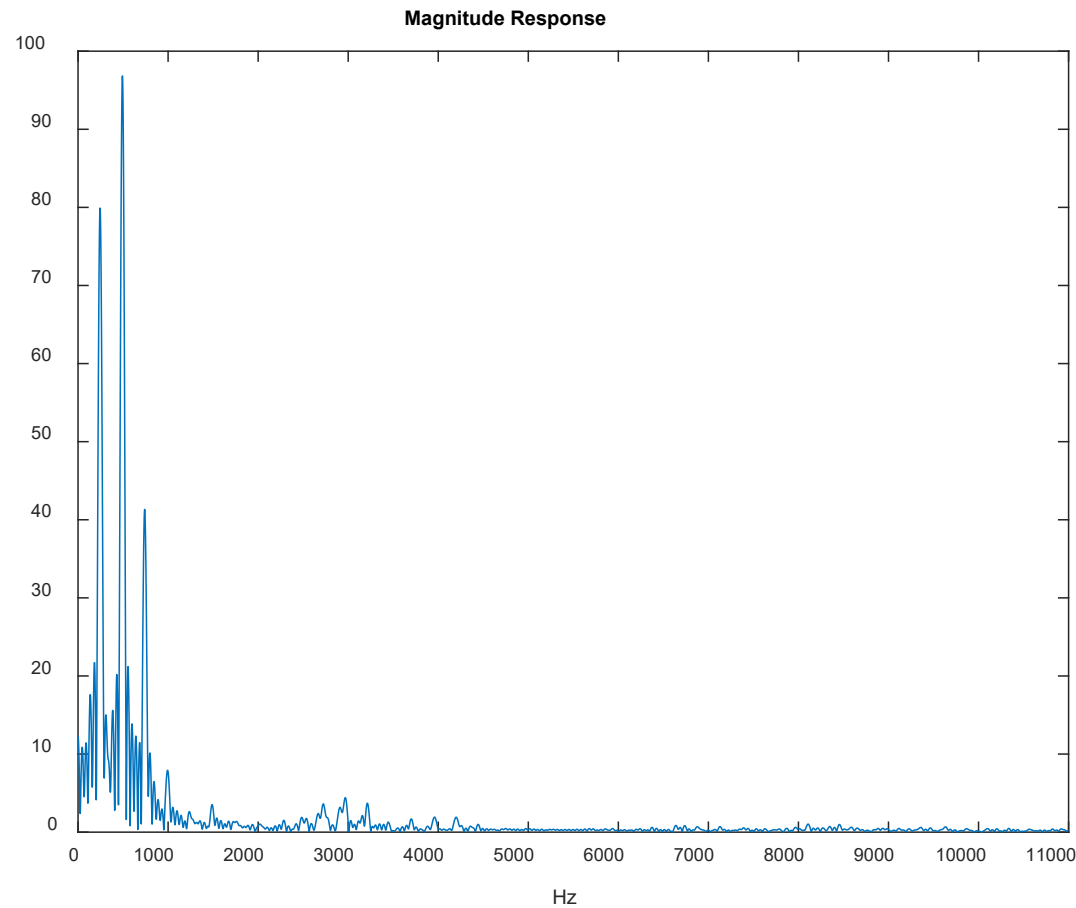


Fig.1.13: Frequency domain representation of speech segment

How to Study?

Make sure you have a clear **concept** and then **practice**.